

Name (Please Print) \_\_\_\_\_

Rec. Instr.

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Your Signature \_\_\_\_\_ Class Time \_\_\_\_\_

ANALYTIC GEOMETRY AND CALCULUS III

Exam III

April 13, 1995

- (16) 1. Find an equation for the tangent plane to the surface  $xyz^3 + yz^2 = 4$  at the point  $P_0 = (1, 2, 1)$ .

Answer \_\_\_\_\_

(16) 2. What does it mean to say that  $f(x, y) = xe^y$  is differentiable at  $P_0 = (1, 0)$ ?

(18) 3. What is the precise rate of change of  $f(x, y, z) = x^3e^y + xz$  at  $P_0 = (4, 0, 16)$  in the direction toward  $P_1 = (2, 1, 4)$ ?

Answer \_\_\_\_\_

(18) 4. Let  $f(x, y) = 3x^2 - 2xy + 5y^2$ . Find and classify the critical points of  $f$ .

(16) 5. Evaluate  $\int_{-1}^1 \int_0^y xye^{x^2} dx dy$ .

Answer \_\_\_\_\_

- (16) 6. Express the double integral of  $f(x, y) = xy^2 + x^2$  over the region  $D$  bounded by the curves  $y = x^2$  and  $x = y^2$  as an iterated integral.